P3635

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[5560]-591 T.E. (I. T.)

THEORY OF COMPUTATION

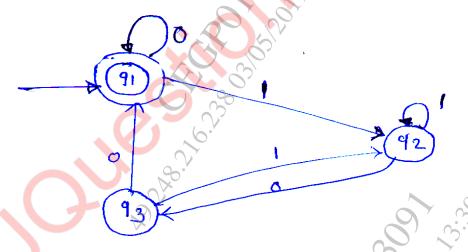
(Semester-I) (314441) (2015 Pattern)

Time: 2½ Hours]

[Max. Marks: 70

Instructions to the candidates:

- 1) Answer Q1 or Q2, Q3 or Q4, Q5 or Q6, Q7 or Q8, Q9 or Q10.
- 2) Neat diagram must be drawn wherever necessary.
- 3) Figures to the right indicate full marks.
- 4) Assume suitable data if necessary.
- Q1) a) Design FA that rear string made up of letters in the word 'CHARIOT' and accept those string that contain 'CAT' as a substring.[5]
 - b) Find out the regular Expression from given transition diagram (FA) by using Arden's theorem. [5]



OR

- **Q2)** a) Show that $L = \{0^i 1^i | i \ge 1\}$ is not regular, by using pumping lemma. [6]
 - b) Define (i) Language-

[4]

With an

Example-(ii) Regular Expression

| Q3) | a) | Find out the CFG From given language "L cantains the strings consisting of a's and b's with at least two a's". [2] | _ |
|-------------|----|---|---|
| | b) | Find the CFL associated with given CFG. [3] | |
| | | $S \rightarrow a A/1/B$ | |
| | | $A \rightarrow 1B/1$ | |
| | | $B \rightarrow 0A/0$ | |
| | b) | Convert the following grammar into (CFF). [5] | |
| | | $S \to ABA$ | |
| | | $A \rightarrow a A \in$ | |
| | | $B \rightarrow b B/\epsilon$ | |
| | | OR | |
| | | | |
| Q4) | a) | Write a short Note on Chansky Hierarch with an example. [4] | 1 |
| | b) | Check whether the following grammar is ambiguous or Not, if it is | |
| | | ambiguous, remove the ambiguity & write an equivalent ambiguous grammar. | |
| | | $S \rightarrow i C t s / i C t s C S$ | • |
| | | $C \rightarrow b, S \rightarrow a$ | |
| | | | |
| Q5) | a) | Construct PDA for following language. [8] | |
| | | $L = \{ 0^{n}1^{m} 2^{n} \mid n, m > = 0 \}$ | V |
| | b) | Design post machine for language. [8] | |
| | | $L = \{ a^n b^n \mid n \geq 1 \}$ | |
| | | OR OR | |
| <i>Q6)</i> | a) | Obtain PDA for given grammar [10] | 1 |
| | | $S \rightarrow a ABC$ | |
| | | $A \rightarrow aB a$ | |
| | | $B \to bA b$ | |
| | | Design post machine for language. $L = \{ a^n b^n \mid n \ge 1 \}$ OR Obtain PDA for given grammar $S \rightarrow a \ ABC$ $A \rightarrow aB \mid a$ $B \rightarrow bA \mid b$ $C \rightarrow a$ Design PDA for following language. | |
| | | Design PDA for following language. | |

b)

[6]

 $L = \{\ a^n\ b^n\ c^m\ d^m\ |\ n,\, m> \ = 1\}$

Q7) a) Design a TM that multiplies two unary. [10] numbers over $\Sigma = \{a\}$ Write simulation for (i) aa & aaa (ii) aaa & aaa

Explain the halting problem in TM. b)

OR

[8]

Construct TM for the language. [10]**Q8**) a) $L = \{ a^n b^n c^n | n > 0 \}$ show simulation for (i) aabbcc (ii) abbccc

- Compare FM, PDA, PM, & TM with respect to language grammar, b) powerfulness and example. [8]
- Prove that following are decidable languages. **Q9**) a) [10]
 - ACFG= { (G, W) | The context sensitive grammar G accepts the input string W}.
 - ADFA = { (B, W) | B accepts the input string W}
 - Prove that pcp with two lists x = (01, 1, 1)b) $y = (01^2, 10, 1^1)$ has no solution.
- Show that HALT $_{TM} = \{ (M, W) \mid \text{The turing Machine M holts on input W} \}$ is *Q10*) a) undecidable. [8]
 - b) Prove that "It is undecidable whether a CFG is ambiguous' [8]