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S.E. (Computer Engineering/IT) (II Sem.) EXAMINATION, 2017 ENGINEERING MATHEMATICS—III

(2015 **PATTERN**)

Time: Two Hours

Maximum Marks: 50

- N.B. :— (i) Answer Q. No. 1 or Q. No. 2, Q. No. 3 or Q. No. 4, Q. No. 5 or Q. No. 6, Q. No. 7 or Q. No. 8.
 - (ii) Neat diagrams must be drawn wherever necessary.
 - (iii) Figures to the right indicate full marks.
 - (iv) Your answers will be valued as a whole.
 - (v) Use of electronic pocket calculator is allowed.
 - (vi) Assume suitable data, if necessary.
- 1. (a) Solve any two of the following:

[8]

- (i) $\frac{d^2y}{dx^2} y = \frac{2}{1 + e^x}$ (use method of variation of parameters)
- (ii) $(D^2-4)y = e^{4x} + 2x^3$
- (iii) $(2x+1)^2 \frac{d^2y}{dx^2} 2(2x+1) \frac{dy}{dx} 12y = 24x$

(*b*) Solve the following integral equation using Fourier transform: [4]

$$\int_0^\infty f(x)\sin \lambda x d\lambda = 1 - \lambda, \ 0 \le \lambda \le 1$$
$$= 0 \quad , \ \lambda \ge 1$$
$$Or$$

An electrical circuit consists of an inductance 0.1 henry, a 2. (a) registance R of 20 ohms and a condenser of capacitance C of 25 microfarads. If the differential equation of electric circuit [4]

$$L\frac{d^2q}{dt^2} + R\frac{dq}{dt} + \frac{q}{C} = 0,$$

then find the charge q and current i at any time t, given that when t = 0, q = 0.05 columbs and $i = \frac{dq}{dt} = 0$.

- Solve any one: (*b*) [4]
 - (*i*) Find:

$$z^{-1} \left\{ \frac{1}{(z-4)(z-5)} \right\}$$

by inversion integral method.

Find z transform of: (ii)

$$f(k) = (k+1) a^k, k \ge 0.$$

Using z transform, solve the following difference equation: [4] (c)

$$f(k+1) + \frac{1}{2}f(k) = \left(\frac{1}{2}\right)^k, k \ge 0$$

$$f(0) = 0.$$

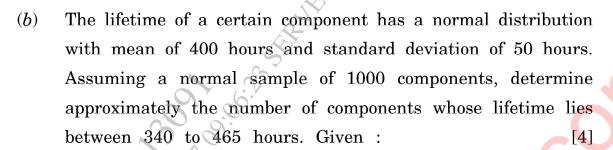
- 3. (a) The first four moments of a distribution about the value 4 of the variable are -1.5, 17, -30 and 108. Find the central moments, β_1 and β_2 . [4]
 - (b) By the method of least squares, find the straight line that best fits the following data: [4]

C 5	\boldsymbol{x}	${oldsymbol y}$
	1	14
232	2	27
	3	40
	4	55
	5	68

- (c) There is a small chance of 1/1000 for any computer produced to be defective. Determine in a sample of 2000 computers, the probability:
 - (i) no defective and
 - (ii) 2 defectives.

Or

- 4. (a) Team A has a probability of $\frac{2}{3}$ of winning whenever the team plays a particular game. If team A plays 4 games, find the probability that the team wins : [4]
 - (i) exactly two games and
 - (ii) at least two games.



$$Z = 1.2 \text{ Area} = 0.3849$$

$$Z = 1.3$$
 Area = 0.4032 .

(c) Calculate the coefficient of correlation for the following data: [4]

\boldsymbol{x}		y
10		18
14		12
18	16.40	24
22	A SOLO	6
22	1/02,	30
30		36

5. (a) Find the directional derivative of a function: [4]

$$\phi = 2x^2 + 3y^2 + z^2$$
 at (2, 1, 3)

in the direction of (i+j+k).

(b) Show that the vector field:

$$\overline{F} = (x+2y+4z)i + (2x-3y-z)j + (4x-y+2z)k$$

is irrotational and hence find a scalar potential function φ such that $\; \overline{F} = \nabla \varphi \, .$

[4]

Find the work done by a force field: [5](c) $\overline{F} = x^2 i + (x - y)j + (y + z)k$

along a straight line from (0, 0, 0) to (2, 1, 2).

Find the directional derivative of: [4] 6. (a) $\phi = 4xz^3 - 3x^2y^2z$ at (1, 1, 1)

in the direction of a vector 3i-2j+k.

- Show that (any one): [4](*b*)
 - $\nabla \left(\frac{\overline{a}.\overline{r}}{r^3} \right) = \frac{\overline{a}}{r^3} \frac{3(\overline{a}.\overline{r})\overline{r}}{r^5}$

where \bar{a} is a constant vector.

- $\nabla^4(r^4) = 120.$ (ii)
- Evaluate the integral (c) [5] $\int \bar{F} \cdot d\bar{r}$

along the curve x = y = z = t from t = 0 to t = 2 where $\overline{F} = (x^2 + yz)i + (y^2 + zx)j + (z^2 + xy)k$

 $\oint \frac{z+4}{(z+1)(z+2)} dz$ circle |z| < 3. [4]7. If (a)

find v such that f(z) = u + iv is analytic.

(*b*) Evaluate: [5]

where C is the circle |z| < 3.

(c) Find the bilinear transformation which maps the points (1, i, -1) from the z plane into the points (i, 0, -i) of the w plane. [4]

Or

8. (a) If [4]

$$u = 3x^2 - 3y^2 + 2y,$$

find v such that f(z) = u + iv is analytic. Determine f(z) in terms of z.

(b) Evaluate: [5]

$$\oint_C \frac{Az^2 + z}{z^2 - 1} dz$$

wehre C is the contour $|z-1| = \frac{1}{2}$.

(c) Find the map of straight line y = x under the transformation

$$w = \frac{z-1}{z+1}.$$

[4]

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